

# MULTIPLYING & DIVIDING

## *Radical Expressions*

When multiplying radicals, multiply the coefficients and multiply the radicands. We can only multiply radicals if they have the same index.

$$\begin{aligned}\text{Ex. 1: } & (2\sqrt{7})(4\sqrt{75}) \\ & (2\sqrt{7})(4\sqrt{25x3}) \\ & (2\sqrt{7})(20\sqrt{3}) \\ & (40\sqrt{21})\end{aligned}$$

Ex. 2: Multiply the following. Remember to simplify the products when possible.

a)  $5\sqrt{3}(\sqrt{6})$

b)  $(-3\sqrt{2x})(4\sqrt{6})$

c)  $7\sqrt{3}(5\sqrt{5} - 6\sqrt{3})$

d)  $-2^3\sqrt[3]{11}(4^3\sqrt{2} - 3^3\sqrt{3})$

## Multiplying and Dividing Radicals

Ex. 3: Multiply the following binomials.

a)  $(8\sqrt{2} - 5)(9\sqrt{5} + 6\sqrt{10})$     b)  $(4\sqrt{2} + 3)(\sqrt{7} - 5\sqrt{14})$

## Multiplying and Dividing Radicals

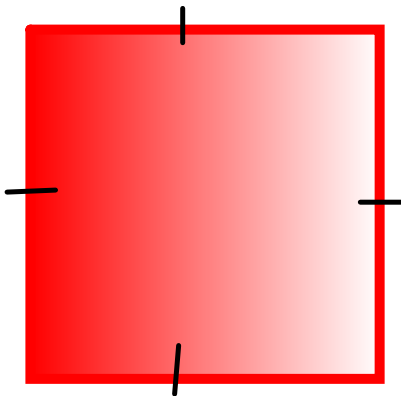
What's the area?

$$7\sqrt{2} + 5\sqrt{3}$$



$$2\sqrt{2} - \sqrt{3}$$

$$6\sqrt{3} + 2$$





When dividing radicals, divide the coefficients and then divide the radicands. Remember, you can only divide radicals that have the same index.

$$\text{Ex. 1: } \frac{4\sqrt[3]{6}}{2\sqrt[3]{3}} = 2\sqrt[3]{2}$$

There are several levels of difficulty when dividing radicals:

### Level 1: "Just Do It"

$$1. \frac{\sqrt{100}}{\sqrt{25}} =$$

$$2. \frac{\sqrt{21}}{\sqrt{3}} =$$

$$3. \frac{\sqrt{20}}{\sqrt{5}} =$$

$$4. \frac{4\sqrt{3}}{\sqrt{3}} =$$

$$5. \frac{24\sqrt[3]{21}}{6\sqrt[3]{3}} =$$

**THiNK**  
**About It.**

Level 2: Doesn't work out evenly - rationalize the denominator

<http://www.khanacademy.org/math/algebra/exponents-radical>



1.  $\frac{4\sqrt{3}}{\sqrt{2}} =$

2.  $\frac{2\sqrt{2}}{\sqrt{3}} =$

3.  $\frac{2\sqrt{6}}{\sqrt{5}} =$

5.  $\frac{3\sqrt{5}}{2\sqrt{6}} =$



**Rationalize:** to convert to a rational number without changing the value of the expression.

Level 3: Rationalizing with binomials as numerators

$$1. \frac{2\sqrt{2} + 3\sqrt{3}}{3\sqrt{6}} =$$

$$2. \frac{\sqrt{7} - 4}{2\sqrt{3}} =$$

$$3. \frac{2\sqrt{3} - 3\sqrt{2}}{\sqrt{2}} =$$





Level 4: Rationalizing with binomials as denominator  
(Conjugate Method)

1.  $\frac{3\sqrt{2}}{2\sqrt{2} - 3} =$

2.  $\frac{3}{\sqrt{5} - \sqrt{2}} =$

3.  $\frac{2}{\sqrt{2} + \sqrt{3}} =$

4.  $\frac{\sqrt{5}}{\sqrt{2} + 3\sqrt{3}} =$



Conjugates: two binomial factors whose product is a difference of squares.

Level 5: Binomials as Numerator & Denominator

$$1. \frac{3\sqrt{2} + 2\sqrt{3}}{\sqrt{2} - \sqrt{8}} =$$

$$2. \frac{3\sqrt{5} - 2\sqrt{3}}{3\sqrt{5} + 2\sqrt{3}} =$$



## Multiplying and Dividing Radicals

### Key Ideas

- When multiplying radicals with identical indices, multiply the coefficients and multiply the radicands:

$$(m\sqrt[k]{a})(n\sqrt[k]{b}) = mn\sqrt[k]{ab}$$

where  $k$  is a natural number, and  $m$ ,  $n$ ,  $a$ , and  $b$  are real numbers.

If  $k$  is even, then  $a \geq 0$  and  $b \geq 0$ .

- When dividing two radicals with identical indices, divide the coefficients and divide the radicands:

$$\frac{m\sqrt[k]{a}}{n\sqrt[k]{b}} = \frac{m}{n}\sqrt[k]{\frac{a}{b}}$$

where  $k$  is a natural number, and  $m$ ,  $n$ ,  $a$ , and  $b$  are real numbers.

$n \neq 0$  and  $b \neq 0$ . If  $k$  is even, then  $a \geq 0$  and  $b > 0$ .

- When multiplying radical expressions with more than one term, use the distributive property and then simplify.
- To rationalize a monomial denominator, multiply the numerator and denominator by an expression that produces a rational number in the denominator.

$$\frac{2}{\sqrt[5]{n}} \left( \frac{(\sqrt[5]{n})^4}{(\sqrt[5]{n})^4} \right) = \frac{2(\sqrt[5]{n})^4}{n}$$

- To simplify an expression with a square-root binomial in the denominator, rationalize the denominator using these steps:
  - Determine a conjugate of the denominator.
  - Multiply the numerator and denominator by this conjugate.
  - Express in simplest form.